

Name _____ Rec. Instr. _____
 Signature _____ Rec. Time _____

Math 220
 Exam 1
 February 2, 2017

No books, calculators, or notes are allowed. Please make sure that your cell phone is turned off. You will have 75 minutes to complete the exam.

SHOW YOUR WORK!

Problem	Points	Points Possible	Problem	Points	Points Possible
1		12	7		8
2		12	8		8
3		4	9		10
4		8	10		10
5		4	11		16
6		8	Total Score		100

1. (4 points each) Evaluate the following limits.

A. $\lim_{x \rightarrow 5} (x^2 + x)$

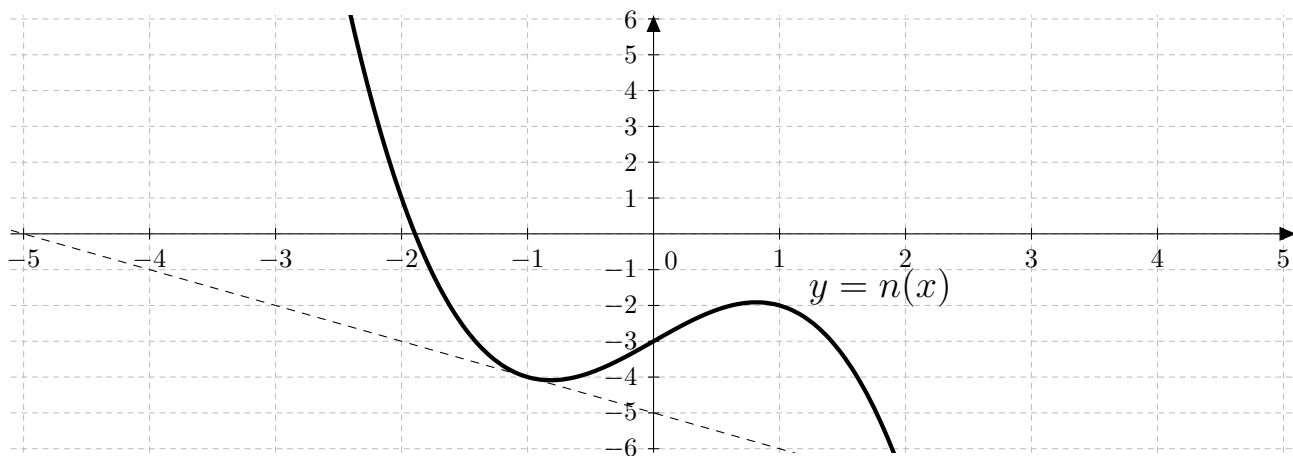
B. $\lim_{\theta \rightarrow 0} \frac{\sin(\theta)}{2\theta}$

C. $\lim_{\theta \rightarrow \pi} \frac{\cos(\theta)}{\theta}$

2. (6 points each) Evaluate the following limits.

A. $\lim_{t \rightarrow 2} \frac{t^2 - 2t}{t - 2}$

B. $\lim_{x \rightarrow 1} \frac{1 - \sqrt{x}}{1 - x}$



3. (2 points each) The function $y = n(x)$ is graphed above in solid bold. There is also a dotted line graphed. Find the following two values.

A. $n(-1) =$

B. $n'(-1) =$

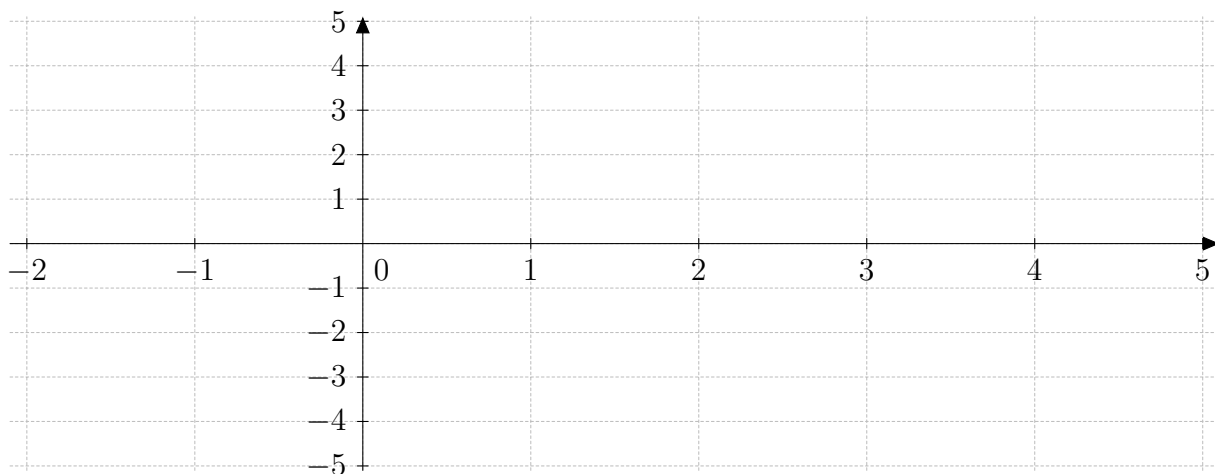
4. (8 points) Use the Intermediate Value Theorem to show that there is a root of $f(x) = x^3 + 2x - 1$ in the interval $(0, 1)$. (**Make sure to mention any properties of $f(x)$ required to apply the Intermediate Value Theorem.**)

5. (4 points) Find functions $h(x)$ and $k(x)$ such that $h(k(x)) = \ln(3x^2 + 4)$.

$h(x) =$

$k(x) =$

6. (8 points) Sketch the graph of $y = 3 \cos(\pi x) + 1$.



7. (4 points each) Given that $\lim_{x \rightarrow 5} u(x) = 8$ and $\lim_{x \rightarrow 5} w(x) = 2$, find the following limits.

A. $\lim_{x \rightarrow 5} \frac{w(x) + 6}{u(x)}$

B. $\lim_{x \rightarrow 5} \frac{\sqrt{u(x) \cdot w(x)}}{x}$

8. (8 points) Find $\lim_{x \rightarrow 0} x^2 \sin\left(\frac{5}{x}\right)$. (Justify your reasoning, and state the name of any theorem used.)

9. Let $v(x) = x^2$.

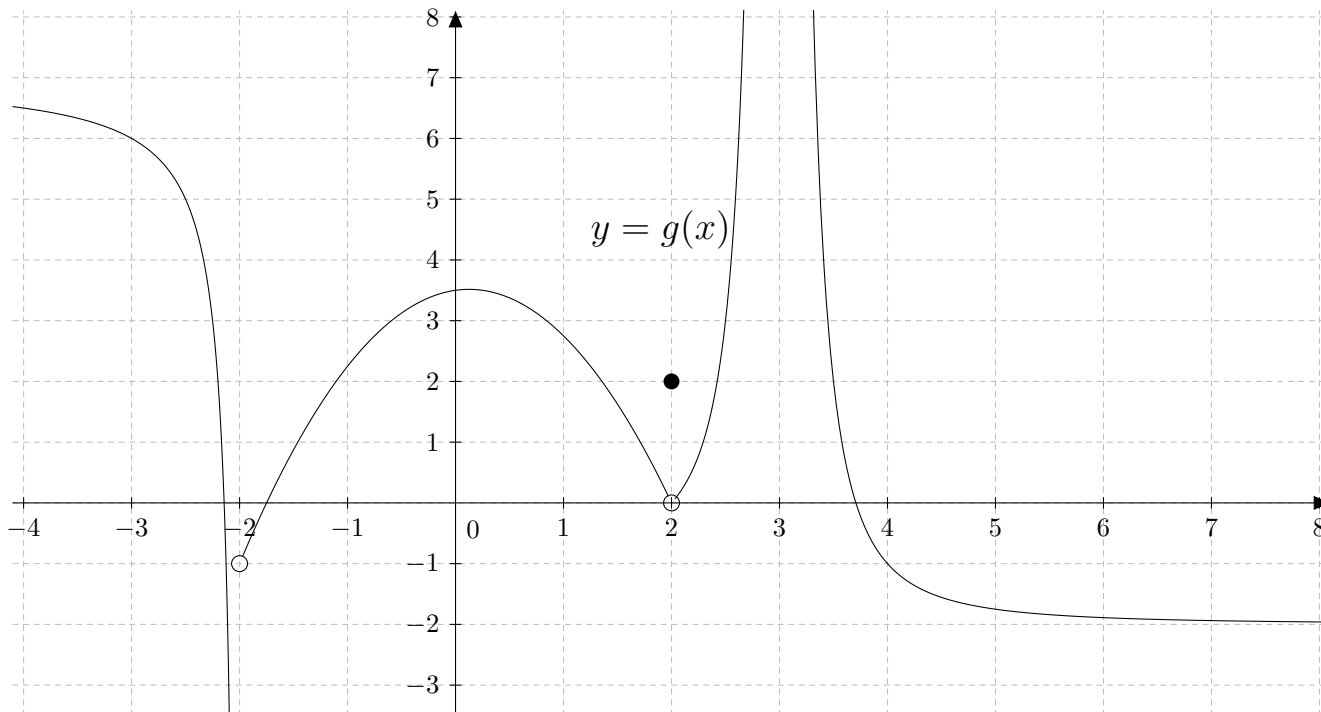
A. (6 points) Using the limit definition of the derivative, find $v'(3)$.

B. (4 points) Find the equation of the tangent line to $y = v(x)$ at $x = 3$.

10. Suppose that an object is at position $s(t) = \frac{1}{t}$ feet at time t seconds.

A. (4 points) Find the average velocity of the object over a time interval from time 3 seconds to time $3 + h$ seconds.

B. (6 points) Find the instantaneous velocity of the object at time 3 seconds by taking the limit of the average velocity in Part A as $h \rightarrow 0$.



11. (2 points each) Consider the graph of $y = g(x)$ above. State the value of each of the below quantities. If the quantity does not exist, write “does not exist”.

A. $\lim_{x \rightarrow -2^-} g(x)$

E. $\lim_{x \rightarrow 2^-} g(x)$

B. $\lim_{x \rightarrow -2^+} g(x)$

F. $\lim_{x \rightarrow 2^+} g(x)$

C. $\lim_{x \rightarrow -2} g(x)$

G. $\lim_{x \rightarrow 2} g(x)$

D. $g(-2)$

H. $g(2)$