Name	Rec. Instr
Signature	Rec Time

Math 220 Exam 2 October 24, 2019

No books, calculators, or notes are allowed. Please make sure that your cell phone is turned off. You will have 75 minutes to complete the exam. Unless instructed otherwise, show your work on each problem.

Problem	Points	Points Possible	Problem	Points	Points Possible
1		12	6		10
2		8	7		12
3		10	8		6
4		10	9		6
5		10	10		16

Total Score	

1. (4 points each) Find the following quantities. You do not need to simplify your answers or show your work. However, showing your work may help you earn partial credit if your answer is incorrect. Recall that $\arctan(z)$ is the inverse trigonometric function $\tan^{-1}(z)$.

A.
$$\frac{d}{dx} \left(\ln(x^3 + 7) \cdot \arctan(x^2 + 5) \right)$$

$$\mathbf{B.} \ \frac{d}{dx} \left(\frac{2^x + 5}{e^x + 1} \right)$$

C.
$$\lim_{x \to -\infty} \frac{2x^8 - x^2 + 3}{7x^9 + 14x + 6}$$

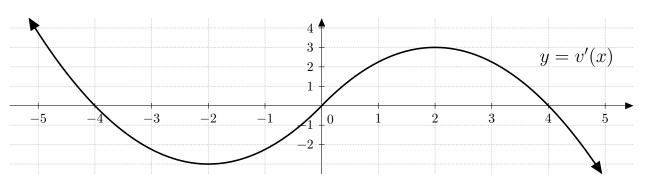
2. (8 points) Let s(t) denote the position of a particle in cm after t seconds. Suppose that we are unable to write down a nice formula for s(t), but we happen to know that when t=1 second, the particle has position 5 cm and velocity 2 cm/s. Find the linearization of s(t) at t=1, and use it to approximate the location of the particle when t=0 seconds. (Include units with your answer.)

3. (10 points) A 5 foot ladder is leaning against a wall. If the top slips down the wall at a rate of 2 ft/s, how fast will the bottom of the ladder be moving away from the wall when the top is 3 feet above the ground? (Include the units.)

4. (10 points) If $\sin(xy) = x^2$, compute $\frac{dy}{dx}$ in terms of x and y.

5. (10 points) Find the absolute maximum and absolute minimum of $w(x) = x^3 - 3x + 2$ on [0, 2].

6. (10 points) Find the derivative of $h(x) = x^{\cos(x)}$.



- 7. (3 points each) y = v'(x) is plotted above. Find:
 - **A.** Interval(s) where v(x) is increasing: ______ decreasing: ______
 - **B.** x-coordinate(s) where v(x) has a local max: ______ local min: _____
 - C. Interval(s) where v(x) is concave up: _____ concave down: _____
 - **D.** x-coordinate(s) where v(x) has an inflection point:
- 8. (3 points each) In each of the following blanks, fill in "max" or "min".
 - **A.** If h'(2) = 0 and $h''(2) = -\frac{\pi}{3}$, then h(x) has a local _____ at x = 2.
 - **B.** If h'(7) = 0 and $h''(7) = \sqrt{2}$, then h(x) has a local _____ at x = 7.
- **9.** (6 points) The volume of a sphere is $V = \frac{4}{3}\pi r^3$, where r denotes the radius. Find the differential dV in terms of r and dr.

10. The function f(x) and its first and second derivatives are:

$$f(x) = \frac{x^2 - 1}{x^2 + 3}$$

$$f'(x) = \frac{8x}{(x^2+3)^2}$$

$$f(x) = \frac{x^2 - 1}{x^2 + 3}$$
 $f'(x) = \frac{8x}{(x^2 + 3)^2}$ $f''(x) = \frac{-24(x^2 - 1)}{(x^2 + 3)^3}$.

Find the information below about f(x), and use it to sketch the graph of f(x). When appropriate, write NONE. No work needs to be shown on this problem.

- A. (1 point) Domain of f(x):
- **B.** (1 point) *y*-intercept: _____
- **C.** (1 point) *x*-intercept(s): _____
- **D.** (1 point) Horizontal asymptote(s):
- **E.** (1 point) Interval(s) f(x) is increasing:
- **F.** (1 point) Interval(s) f(x) is decreasing:
- G. (1 point) Local maximum(s) (x, y):
- **H.** (1 point) Local minimum(s) (x, y):
- I. (1 point) Interval(s) f(x) is concave up:
- **J.** (1 point) Interval(s) f(x) is concave down:
- **K.** (1 point) Inflection point(s) (x, y):
- **L.** (5 points) Sketch y = f(x) on the graph below.

