

Math 221
Summer 2016
Final

7/29/16

Time Limit: 75 Minutes

Name (Print): _____

Teaching Assistant _____

During this exam you may *not* use your books, notes, or any calculator.

You are required to show your work on each problem on this exam. The following rules apply:

- **If you use a theorem you must indicate this and explain** why the theorem may be applied.
- **Organize your work**, in a reasonably neat and coherent way, in the space provided.
- If you need more space, use the back of the pages; clearly indicate when you have done this.

Do not write in the table to the right.

Problem	Points	Score
1	20	
2	20	
3	20	
4	20	
5	20	
6	20	
7	20	
8	20	
9	20	
Total:	180	

1. (20 points) Compute the following integral.

$$\int_0^1 x e^x dx$$

2. (20 points) Compute the following integral.

$$\int \frac{x^5}{\sqrt{1+x^2}} dx$$

3. (20 points) Compute the following integral.

$$\int \frac{x^2 + x}{x - 2} dx$$

4. (20 points) Compute the following integral if it exists.

$$\int_1^2 x \ln(x^2 - 1) dx$$

5. (20 points) Determine if the following series converges or diverges.

$$\sum_{n=1}^{\infty} \frac{n^2}{\sqrt{n^4 + 1}}$$

6. (20 points) Determine if the following series converges or diverges.

$$\sum_{n=1}^{\infty} \frac{1}{e^n - \ln n}$$

7. (20 points) Determine if the following series converges or diverges.

$$\sum_{n=1}^{\infty} \frac{\cos n}{n^2 + 1}$$

8. (20 points) Find the Taylor Series Expansion for the following function centered at $c=5$.

$$f(x) = \frac{x^2}{9 + 3x}$$

9. (20 points) Express the following equation in terms of rectangular coordinates. $r = \sin \theta$.