

NAME \_\_\_\_\_

Rec. Instructor: \_\_\_\_\_

Signature \_\_\_\_\_

Rec. Time \_\_\_\_\_

**CALCULUS II - FINAL EXAM Part 2**  
**August 2, 2019**

Show all work for full credit. No books, notes or calculators are permitted. The point value of each problem is given in the left-hand margin. You have 1 hour and 15 minutes.

Problem	Points	Points Possible	Problem	Points	Points Possible
1		10	6		10
2		10	7		10
3		10	8		10
4		10	9		10
5		10	Total Score		200

$$\tfrac{d}{dx}\tan x=\sec^2x\qquad\qquad \tfrac{d}{dx}\sec x=\sec x\tan x\qquad\qquad \tfrac{d}{dx}b^x=b^x\ln(b)$$

$$\tfrac{d}{dx}\sin^{-1}(x)=\tfrac{1}{\sqrt{1-x^2}}\qquad\qquad \tfrac{d}{dx}\tan^{-1}(x)=\tfrac{1}{1+x^2}\qquad\qquad \tfrac{d}{dx}\sec^{-1}(x)=\tfrac{1}{|x|\sqrt{x^2-1}}$$

$$\int \tan x ~dx = -\ln |\cos x| + C \qquad\qquad \int \sec x ~dx = \ln |\sec x + \tan x| + C$$

$$\int \frac{dx}{\sqrt{a^2-x^2}}=\sin^{-1}(\frac{x}{a})+C\qquad\qquad \int \frac{dx}{a^2+x^2}=\frac{1}{a}\tan^{-1}(\frac{x}{a})+C$$

$$\int \sin^n x ~dx=-\frac{\sin^{n-1}x\cos x}{n}+\frac{n-1}{n}\int \sin^{n-2}x ~dx,$$

$$\int \cos^n x ~dx=\frac{\cos^{n-1}x\sin x}{n}+\frac{n-1}{n}\int \cos^{n-2}x ~dx,$$

$$\int \tan^n x ~dx=\frac{\tan^{n-1}x}{n-1}-\int \tan^{n-2}x ~dx\,,$$

$$\int \sec^n x ~dx=\frac{\sec^{n-2}x\tan x}{n-1}+\frac{n-2}{n-1}\int \sec^{n-2}x ~dx$$

$$M_x=\tfrac{1}{2}\int_a^bf(x)^2-g(x)^2~dx\,,\quad M_y=\int_a^bx(f(x)-g(x))~dx\,.$$

$$|R_n(x)|\leq \tfrac{K}{(n+1)!}|x-a|^{n+1}\,,\text{ with }\, K=\max_{a\leq c\leq x}|f^{(n+1)}(c)|\,.$$

$$\tfrac{1}{1-x}=\sum\nolimits_{n=0}^\infty x^n\,,\quad\; e^x=\sum\nolimits_{n=0}^\infty \tfrac{x^n}{n!},\quad\;\ln(1+x)=\sum\nolimits_{n=1}^\infty \tfrac{(-1)^{n+1}x^n}{n}$$

$$\sin x=\sum\nolimits_{n=0}^\infty \tfrac{(-1)^nx^{2n+1}}{(2n+1)!},\quad\;\cos x=\sum\nolimits_{n=0}^\infty \tfrac{(-1)^nx^{2n}}{(2n)!}$$

$$\int_a^b \sqrt{1+(dy/dx)^2}~dx\,,\quad \int_a^b 2\pi r\sqrt{1+(dy/dx)^2}~dx.$$

$$\int_a^b y(t) x'(t)~dt\,,\quad \int_a^b \sqrt{x'(t)^2+y'(t)^2}~dt\,,~\int_a^b 2\pi r\sqrt{x'(t)^2+y'(t)^2}~dt\,,$$

$$\tfrac{1}{2}\int_a^b r^2~d\theta\,,~\int_a^b \sqrt{r(\theta)^2+r'(\theta)^2}~d\theta\,,~~\int_a^b \sqrt{r^2+\left(\tfrac{dr}{d\theta}\right)^2}d\theta$$

(10)

1. Consider the curve with parametric equations  $x = 4t^3 - t^2$  and  $y = t^2 + 2t$

(a) For which values of  $t$  is the slope horizontal?

(b) For which values of  $t$  is the slope vertical?

(c) What is the area from  $1 \leq t \leq 2$ ?

(10)

**2.** Evaluate the improper integral or show that it diverges

$$\int_0^{\infty} xe^{-5x^2} dx$$

(10)

- 3.** Does the series conditionally converge, absolutely converge, or diverge? Name all tests used.

$$\sum_{n=1}^{\infty} \frac{\cos(\pi n)}{n}$$

(10)

- 4.**  $\sum_{n=2}^{\infty} \frac{4n^2 + 1}{3n + 2n^5}$

- (10) **5.** (a) Convert the polar equation  $r = 4 \sin(\theta)$  to a rectangular or cartesian equation.

(b) Find the arc length in polar coordinates for polar equation part (a) from  $0 \leq \theta \leq \pi$ .

(10)

6. Find the interval of convergence of the power series  $\sum_{n=1}^{\infty} \frac{(x+2)^n}{n! 3^n}$ . (Make clear the status of any end points.)

(10)

7.  $\int x^4 \ln|x| dx$

(10)

8.  $\int \frac{dx}{3+x^2}$

- (10)
9. Does the series conditionally converge, absolutely converge, or diverge? Name all tests used.
- $$\sum_{n=1}^{\infty} (-1)^n \frac{n!}{3n!}$$