

Name:

Recitation Instructor, Day, Time:

## TRADITIONAL MATH 100 – Exam 2 – March 2016

**Directions:** You will find 14 problems listed below. No notes/books/friends are allowed. Graphing calculator models above the level of a TI-84 plus are not allowed. You have one hour to complete this exam.

Page 1 20 pts.	Page 2 20 pts.	Page 3 20 pts.	Page 4 20 pts.	Page 5 20 pts.	TOTAL 100 pts

1. (6 points) Find the solutions and check your answers:  $8 - 2|x + 5| = 12$ .

2. (6 points) Find the solutions to  $3x^2 - x - 8 = 0$ .

3. (8 points) Solve the quadratic inequality  $x^2 + 5x < 6$ .

4. (8 points) In a controlled lab environment, some organisms exhibit constant growth over a specific time period. Suppose a certain organism starts out weighing 1 mg, and grows to 11 mg over a 20 hour time period. Find a linear model (in other words, find a linear function) that describes the growth of the organism for  $0 \leq t \leq 20$  hours.
5. (6 points) Find an equation of the line passing through  $(-2, 7)$  and parallel to  $x + 4y = 3$ .
6. (6 points) Find the quotient and remainder when  $p(x) = 5x^3 - 2x + 1$  is divided by  $x^2 + 3x - 5$ . Write  $p(x)$  in the form  $d(x)q(x) + r(x)$ , where  $d(x)$ ,  $q(x)$  and  $r(x)$  are the divisor, quotient and remainder, respectively.

7. (5 points) Suppose the number of vehicle thefts in a given area, from the years 1960 to 1990, could be modeled by the polynomial  $p(x) = 30.97x^3 - 1266.9x^2 + 19199x + 29,130$ , where  $x$  is the number of years since 1960. What is  $p(0)$ , and what is its meaning in context of the model? Explain in a brief sentence.
8. (5 points) Find the vertex of the quadratic function  $C(x) = x^2 - 400x + 6200$ . Is the vertex a maximum or minimum, and how do you know?
9. (10 points) Consider the polynomial  $p(x) = -4x^4 - 6x^3 + 2x + 400$ . Circle TRUE or FALSE for each of the statements below.
- |     |      |       |  |
|-----|------|-------|--|
| (a) | TRUE | FALSE | $p(x)$ has odd degree.                                   |
| (b) | TRUE | FALSE | $p(x)$ has a positive y-intercept.                       |
| (c) | TRUE | FALSE | $p(x)$ has positive leading coefficient.                 |
| (d) | TRUE | FALSE | As $x \rightarrow \infty$ , $p(x) \rightarrow \infty$ .  |
| (e) | TRUE | FALSE | As $x \rightarrow -\infty$ , $p(x) \rightarrow \infty$ . |

10. (8 points) A parabola has vertex at  $(5, 4)$  and passes through the point  $(-6, 1)$ . What is the equation of the parabola? Write your answer in the form  $y = ax^2 + bx + c$ .
11. (6 points) Using the **REMAINDER THEOREM**, find  $p(3)$  when  $p(x) = 4x^4 + x^2 - x + 3$ . Be sure to identify your final answer.
12. (6 points) Consider two quadratic functions given by  $f(x) = 2x^2 - 11x + 12$  and  $g(x) = x^2 - 3x + 5$ . Find the intersection points of these two parabolas and state your answers as ordered pairs.

13. (6 points) Solve:  $|4x - 3| < 8$ .

14. (6 points) Solve:  $|2x - 7| > 4$ .

15. (8 points) Consider the parabola  $f(x) = (x + 2)^2 + 5$ . Answer the following questions. (Drawing a quick sketch of the graph of  $f(x)$  may help you.)

(a) What is the domain of  $f(x)$ ?

(b) What is the vertex of  $f(x)$ ?

(c) What is the range of  $f(x)$ ?

(d) What is the axis of symmetry of  $f(x)$ ?