

Recitation Instructor, Day, Time:

TRADITIONAL MATH 100 – Final Exam – Summer 2017

**Directions:** You will find 11 problems listed below. No notes/books/friends are allowed. Graphing calculator models above the level of a TI-84 plus are not allowed. You have one hour to complete this exam.

- (7 points) Find the equation of the line connecting the two points  $(-4, 7)$  and  $(5, 12)$ .
- (8 points) Suppose the cost function for a certain product is given by  $C(x) = 16x + 3900$  and the revenue function for the product is given by  $R(x) = 45x$ . Find a formula for the following functions:
  - Profit Function,  $P(x)$
  - Average Cost Function,  $\overline{C(x)}$
- (8 points) Given  $g(x) = x^2 - 4x$  and  $h(x) = 7x + 9$ , find the following:
  - $(hg)(x)$
  - $h(g(x))$

4. (10 points) The cost function  $C(x) = 2x^2 - 800x + 102000$  describes the cost, in dollars, of making  $x$  units of a certain product. What is the vertex of this quadratic function? Show your work with algebra. If you choose to use a graph as part of your work, you must include a graph having the pertinent information that helps to answer this question.

5. (8 points) Solve and check:  $x - 4 = \sqrt{4x - 20}$

6. (8 points) Find a rational function with the following features: (a) horizontal asymptote at  $y = 0$ ; (b) poles at  $x = 4$  and  $x = -2$ ; (c) zeros at  $x = 1$  and  $x = -1$ .

7. (9 points) Fill in the blank:

(a)  $\log_3\left(\frac{1}{81}\right) = \underline{\hspace{2cm}}$

(b)  $\log_2(64) = \underline{\hspace{2cm}}$

(c)  $\log_b(b^2) = \underline{\hspace{2cm}}$

8. (8 points) Suppose \$200 is invested in an account paying 1.5% annual interest, compounded continuously. Using an exponential growth model,  $P(t) = P_0e^{kt}$ , determine the time required for the initial investment to double.

9. (8 points) Solve for  $x$  the equation:  $2e^{x+2} - 3 = 11$ . Leave exact (don't use a calculator).

10. (8 points) Solve the following system using any method except the calculator method:

$$4x - 3y = 8$$

$$5x + 2y = 1$$

11. (8 points) JUST SET UP a system that would help solve the following problem. DO NOT SOLVE IT. Light roast coffee beans cost \$4.00/lb, medium roast coffee beans costs \$1.00/lb, and dark roast coffee beans cost \$4.50/lb. If there is twice as much medium roast as there is of the light roast, how much of each type of coffee is needed to create 5 pounds of a mixture that costs \$3.50 per pound? Be sure to indicate the meaning of any variables used in setting up this problem.