

Name:

Recitation Instructor, Day, Time:

## TRADITIONAL MATH 100 – Exam 3 – November 2019

**Directions:** You will find 13 problems listed below. No notes/books/friends are allowed. Graphing calculator models above the level of a TI-84 plus are not allowed. You have one hour to complete this exam.

| # 1 | # 2 | # 3 | # 4 | # 5 | # 6 | # 7 | # 8 | # 9 | # 10 | # 11 | # 12 | # 13 | TOTAL |
|-----|-----|-----|-----|-----|-----|-----|-----|-----|------|------|------|------|-------|
|     |     |     |     |     |     |     |     |     |      |      |      |      |       |

1. (6 points) Find the domain of the function  $f(x) = \log(4x + 3)$ .

2. (6 points) Solve:  $5 + 4e^{(x+1)} = 13$ . Leave answers exact (in other words, don't use a calculator).

3. (6 points) Using the values  $\log(a) = 10$  and  $\log(b) = 2$ , find  $\log(b^2\sqrt{a})$ .

4. (6 points) Solve:  $3\log_4(5x - 2) - 1 = 8$ . Leave answers exact (in other words, don't use a calculator).

5. (8 points)

(a) Rewrite using the base  $b$  via the change of base formula:

$$\log_R(M) =$$

(b) Condense into a single logarithmic expression using the properties of logarithms (you may assume that  $z$  is positive):  $\log_4(z) + \log_{16}(z + 1)$ .

6. (8 points) Find the domain of the function  $f(x) = \sqrt{x^2 - 3x - 4}$

7. (8 points) Solve and check your answer for the following rational equation:  $\frac{5}{3x+2} = \frac{2}{x-1}$

8. (8 points) Solve the rational inequality:  $\frac{2x-6}{x+1} > 0$ . Be sure to justify your answer using appropriate methods.

9. (6 points) The supply function for a certain product is given by  $p = 30 \cdot (4^q)$ , where  $p$  is the price of the product and  $q$  is the quantity supplied at that price. If the price of the product is \$30,720, how many units will be supplied?

10. (a) (6 points) Find  $f^{-1}(x)$  when  $f(x) = -3x + 5$ .

- (b) (6 points) Find  $g^{-1}(x)$  when  $g(x) = \log_5(x - 3)$ .

11. (6 points) Suppose  $R(t) = 2t$  is a function that gives the radius of a circular oil spill at  $t$  minutes. Given  $A(r) = \pi r^2$ , find an expression for  $A(R(t))$ , and leave your final answer in terms of  $\pi$ .

12. (8 points) Given  $f(x) = 2x^2 + x - 4$  and  $g(x) = 3x + 2$ , find  $f(g(x))$  and write your answer in the form  $ax^2 + bx + c$ .

13. (12 points) Graph  $f(x) = 2^x$  and  $g(x) = \log_2(x)$  on the same grid. Include at least 4 points on each graph and include relevant asymptotes.

